



POSITION OF SUN ON CELESTIAL SPHERE AT INPUT UNIVERSAL TIME (UT)

RC Chakraborty (Retd), Former Director, DRDO, Delhi & Visiting Professor, JUET, Guna,
www.myreaders.info, rcchak@gmail.com,

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POSITION OF SUN ON CELESTIAL SPHERE AT INPUT UNIVERSAL TIME (UT) .

Sun is a star at the center of our Solar System. Although stars are fixed relative to each other, but Sun moves relative to stars.

Sun follows a circular path on the celestial sphere, once a year. This path is known as the 'Ecliptic', representing the plane of the Earth's orbit.

Inclination of the Earth's equator to the Ecliptic (or earth's rotation axis to a perpendicular on ecliptic) is called **Obliquity of the ecliptic**.

The Obliquity of the ecliptic is currently 23.4392794383 deg with respect to the celestial equator, at standard epoch J2000 .

The position of any point on the Celestial Sphere is given with reference to the equator or the ecliptic.

- reference to Equator, the position is specified by Right ascension and Declination.
- reference to Ecliptic, the position is specified by celestial Longitude and Latitude.

The Earth moves in an elliptical orbit around the Sun. Therefore the distance from Earth to Sun is not same at all points on the orbit.

- distance Earth to Sun (d_{sun}) calculated as $r = a(1-e \cos(\theta)) / (1+e \cos(\theta))$ where a = semi-major axis, e = eccentricity and θ = mean anomaly of sun.
- radial distance from Earth to Sun (R_s) calculated as $R = 1.00014 - (0.01671 * \cos g) - (0.00014 * \cos 2g)$ where g = mean anomaly of sun
- mean distance from Earth to Sun = 149,597,870.700 km, called 1 Astronomical Unit, (Ref. http://en.wikipedia.org/wiki/Astronomical_unit)
- minimum distance from Earth to Sun = 147,098,074 km or 0.98 AU, and this point is called Perihelion;
- maximum distance from Earth to Sun = 152,097,701 km or 1.02 AU, and this point is called Aphelion;
- average distance from Earth to Sun (A_s) = 149,597,887.5 km is the distance $(\max + \min)/2$.

(Ref http://wiki.answers.com/Q/What_is_the_distance_between_Earth_and_the_Sun).

At any input Universal Time, to compute the position of Sun and its related traits, the algorithm goes through following steps :

- Find Julian day of interest corresponding to the input Universal Time;**
- Find Corresponding Ecliptic coordinates**
 - Mean anomaly of the Sun (actually, Earth orbits around Sun, but here pretends Sun orbits Earth)
 - Mean Longitude of the Sun;
 - Ecliptic Longitude of the Sun;
 - Ecliptic latitude of the Sun is always nearly zero (the value never exceeds 0.00033 deg)

- Distance of the Sun from the Earth, in astronomical units
- Obliquity of the ecliptic

(c) Find Corresponding Equatorial coordinates

- Right ascension
- Declination

In addition to these Ecliptic and Equatorial coordinates, computed many other parameters related to Sun's Position on Celestial Sphere.

The Position of Sun on Celestial Sphere is represented by computing following parameters :

Semi-major axis (SMA), Mean movement per day (n sun), Mean distance (As), Mean anomaly (m sun), True anomaly (T sun), Eccentric anomaly (E sun), Right ascension (Alpha), Declination (Delta), Mean Longitude (Lmean), Ecliptic longitude (Lsun), Nodal elongation (U sun), Argument of perigee (W sun), Obliquity of ecliptic (Epsilon), Mean dist (d_sun), Radial distance (Rs).

Total 22 parameters computed at Standard Epoch JD2000 (ie YY 2000, MM 1, DD 1, hr 12.00) and at six orbit time event points for YY 2013.

The six orbit events points are when Earth reaches Perihelion & Aphelion, Vernal & Autumnal Equinox, Summer & Winter Solstice.

For any desired year, first computed the Universal time (UT) for earth to reach the respective orbit events point, then apply the same UT as input time for finding the corresponding orbit parameters at that time instnt.

(Note : The orbit events being specific, the values computed can be verified easily with those reported from other sources.)

Move on to Find Position of Sun on Celestial Sphere, the Utilities of OM-MSS Software (Sections - 3.1 to 3.8).

Computing Sun Position on Celestial Sphere at Seven different Time events, respectively :

- (a) Time Event - Standard Epoch JD2000 ;
- (b) Time Event - when Earth at Perihelion ;
- (c) Time Event - when Earth at Vernal equinox ;
- (d) Time Event - when Earth at Summer solstice ;
- (e) Time Event - when Earth at Aphelion ;
- (f) Time Event - when Earth at Autumnal equinox ;
- (g) Time Event - when Earth at Winter solstices ;

Next Section - 3.1 Position of sun at standard epoch time JD2000

SUN Positional Parameters on Celestial Sphere : Input Time (UT) Standard Epoch JD2000

1. Finding Position of Sun on Celestial Sphere at Input UT Standard Epoch time JD2000 .

Input Universal Time Corresponds to Julian Day JD2000 : year = 2000, month = 1, day = 1, hour = 12, minute = 0, seconds = 0.00000

Output : Sun Position on Celestial Sphere Corresponding to input time, JD2000

| | | | | | |
|--|---|-----------------|--|---|-----------------|
| 01. Earth around Sun Mean motion rev per day (mm) | = | 0.0027377786 | 02. Semi-major axis in km considering oblateness (SMA) | = | 149598616.31172 |
| 03. Earth mean motion deg per day using SMA (mm) | = | 0.9856003000 | 04. Sun mean movement deg per day (n sun) | = | 0.9856003000 |
| 05. Eccentricity of earth orbit (e sun) | = | 0.0167102190 | 06. Perihelion to input time diff in Julian days | = | -2.5081161195 |
| 07. Mean anomaly in deg per day from n_sun (m sun) | = | -2.4719999999 | 08. Sun Mean Longitude in deg (Lmean) | = | 280.4600000000 |
| 09. Earth Mean anomaly in deg (ME) | = | 357.5280000000 | 10. Sun Ecliptic Longitude in deg (Lsun) | = | 280.3756801972 |
| 11. Obliquity of ecliptic in deg (Epcylone) | = | 23.4392794444 | 12. Sun Right ascension in deg (Alpha) | = | 281.2858630915 |
| 13. Sun Declination in deg (Delta) | = | -23.0337026521 | 14. Sun Mean distance in km (As) | = | 149598616.31172 |
| 15. Sun Radial distance from earth in km (Rs) | = | 147101227.61694 | 16. Sun Nodal elongation in deg (U sun) | = | -79.6243198028 |
| 17. Sun Mean anomaly in deg (M sun) | = | 357.5280000002 | 18. Sun Eccentric anomaly in deg (E sun) | = | 357.4860040557 |
| 19. Sun True anomaly in deg (T sun) | = | 357.4436516380 | 20. Sun Argument of perigee in deg (W sun) | = | 282.9320285593 |
| 21. Sun True anomaly in deg from U & W (V sun) | = | 357.4436516380 | 22. Sun Distance in km (d sun) | = | 147101040.52850 |

Sun Ecliptic latitude is always nearly zero (the value never exceeds 0.00033 deg)

Next Section - 3.2 Position of sun at time when earth is at perihelion

OM-MSS Section - 3.2

SUN Positional Parameters on Celestial Sphere : Input Year Time when Earth is at Perihelion.

2. Finding Position of Sun on Celestial Sphere at Input Universal Time, when Earth is at Perihelion .

Input Universal Time Corresponds to Earth at Perihelion : year = 2013, month = 1, day = 3, hour = 9, minute = 11, seconds = 56.61639

Output : Sun Position on Celestial Sphere Corresponding to input time, Earth reaching Perihelion

| | | | | | |
|--|---|-----------------|--|---|-----------------|
| 01. Earth around Sun Mean motion rev per day (mm) | = | 0.0027377786 | 02. Semi-major axis in km considering oblateness (SMA) | = | 149598616.31172 |
| 03. Earth mean motion deg per day using SMA (mm) | = | 0.9856003000 | 04. Sun mean movement deg per day (n sun) | = | 0.9856003000 |
| 05. Eccentricity of earth orbit (e sun) | = | 0.0167102190 | 06. Perihelion to input time diff in Julian days | = | 0.0000000000 |
| 07. Mean anomaly in deg per day from n_sun (m sun) | = | 0.0000000000 | 08. Sun Mean Longitude in deg (Lmean) | = | 283.1557666033 |
| 09. Earth Mean anomaly in deg (ME) | = | 0.0000000001 | 10. Sun Ecliptic Longitude in deg (Lsun) | = | 283.1557666033 |
| 11. Obliquity of ecliptic in deg (Epcylone) | = | 23.4375874462 | 12. Sun Right ascension in deg (Alpha) | = | 284.2922173002 |
| 13. Sun Declination in deg (Delta) | = | -22.7872783368 | 14. Sun Mean distance in km (As) | = | 149598616.31172 |
| 15. Sun Radial distance from earth in km (Rs) | = | 147098823.43315 | 16. Sun Nodal elongation in deg (U sun) | = | -76.8442333967 |
| 17. Sun Mean anomaly in deg (M sun) | = | 0.0000000000 | 18. Sun Eccentric anomaly in deg (E sun) | = | 0.0000000000 |
| 19. Sun True anomaly in deg (T sun) | = | 0.0000000000 | 20. Sun Argument of perigee in deg (W sun) | = | 283.1557666033 |
| 21. Sun True anomaly in deg from U & W (V sun) | = | 0.0000000000 | 22. Sun Distance in km (d sun) | = | 147098790.67105 |

Sun Ecliptic latitude is always nearly zero (the value never exceeds 0.00033 deg)

Next Section - 3.3 Position of sun at time when earth is at vernal equinox

SUN Positional Parameters on Celestial Sphere : Input Year Time when Earth is at Vernal equinox .

3. Finding Position of Sun on Celestial Sphere at Input Universal Time, when Earth is at Vernal equinox .

Input Universal Time Corresponds to Earth at Vernal equinox : year = 2013, month = 3, day = 20, hour = 11, minute = 2, seconds = 9.15719

Output : Sun Position on Celestial Sphere Corresponding to input time, Earth reaching Vernal equinox

| | | | | | |
|--|---|-----------------|--|---|-----------------|
| 01. Earth around Sun Mean motion rev per day (mm) | = | 0.0027377786 | 02. Semi-major axis in km considering oblateness (SMA) | = | 149598616.31172 |
| 03. Earth mean motion deg per day using SMA (mm) | = | 0.9856003000 | 04. Sun mean movement deg per day (n sun) | = | 0.9856003000 |
| 05. Eccentricity of earth orbit (e sun) | = | 0.0167102190 | 06. Perihelion to input time diff in Julian days | = | 76.0765340370 |
| 07. Mean anomaly in deg per day from n_sun (m sun) | = | 74.9810547699 | 08. Sun Mean Longitude in deg (Lmean) | = | 358.1404045779 |
| 09. Earth Mean anomaly in deg (ME) | = | 74.9810547700 | 10. Sun Ecliptic Longitude in deg (Lsun) | = | 0.0000000000 |
| 11. Obliquity of ecliptic in deg (Epcylone) | = | 23.4375603478 | 12. Sun Right ascension in deg (Alpha) | = | 0.0000000000 |
| 13. Sun Declination in deg (Delta) | = | 0.0000000000 | 14. Sun Mean distance in km (As) | = | 149598616.31172 |
| 15. Sun Radial distance from earth in km (Rs) | = | 148989898.67840 | 16. Sun Nodal elongation in deg (U sun) | = | 0.0000000000 |
| 17. Sun Mean anomaly in deg (M sun) | = | 74.9810547697 | 18. Sun Eccentric anomaly in deg (E sun) | = | 75.9096738744 |
| 19. Sun True anomaly in deg (T sun) | = | 76.8402303407 | 20. Sun Argument of perigee in deg (W sun) | = | 283.1597696594 |
| 21. Sun True anomaly in deg from U & W (V sun) | = | 76.8402303407 | 22. Sun Distance in km (d sun) | = | 148912015.96700 |

Sun Ecliptic latitude is always nearly zero (the value never exceeds 0.00033 deg)

Next Section - 3.4 Position of sun at time when earth is at summer solsticex

SUN Positional Parameters on Celestial Sphere : Input Year Time when Earth is at Summer solstice .

4. Finding Position of Sun on Celestial Sphere at Input Universal Time, when Earth is at Summer solstice .

Input Universal Time Corresponds to Earth at Summer solstice : year = 2013, month = 6, day = 21, hour = 5, minute = 1, seconds = 19.19999

Output : Sun Position on Celestial Sphere Corresponding to input time, Earth reaching Summer solstice

| | | | | | |
|--|---|-----------------|--|---|-----------------|
| 01. Earth around Sun Mean motion rev per day (mm) | = | 0.0027377786 | 02. Semi-major axis in km considering oblateness (SMA) | = | 149598616.31172 |
| 03. Earth mean motion deg per day using SMA (mm) | = | 0.9856003000 | 04. Sun mean movement deg per day (n sun) | = | 0.9856003000 |
| 05. Eccentricity of earth orbit (e sun) | = | 0.0167102190 | 06. Perihelion to input time diff in Julian days | = | 168.8259558287 |
| 07. Mean anomaly in deg per day from n_sun (m sun) | = | 166.3949127126 | 08. Sun Mean Longitude in deg (Lmean) | = | 89.5586310183 |
| 09. Earth Mean anomaly in deg (ME) | = | 166.3949127126 | 10. Sun Ecliptic Longitude in deg (Lsun) | = | 89.9999483110 |
| 11. Obliquity of ecliptic in deg (Epcylone) | = | 23.4375273104 | 12. Sun Right ascension in deg (Alpha) | = | 89.9999436629 |
| 13. Sun Declination in deg (Delta) | = | 23.4375273104 | 14. Sun Mean distance in km (As) | = | 149598616.31172 |
| 15. Sun Radial distance from earth in km (Rs) | = | 152030583.04072 | 16. Sun Nodal elongation in deg (U sun) | = | 90.0000000000 |
| 17. Sun Mean anomaly in deg (M sun) | = | 166.3949127122 | 18. Sun Eccentric anomaly in deg (E sun) | = | 166.6165253213 |
| 19. Sun True anomaly in deg (T sun) | = | 166.8363660940 | 20. Sun Argument of perigee in deg (W sun) | = | 283.1636339060 |
| 21. Sun True anomaly in deg from U & W (V sun) | = | 166.8363660940 | 22. Sun Distance in km (d sun) | = | 152025947.60113 |

Sun Ecliptic latitude is always nearly zero (the value never exceeds 0.00033 deg)

Next Section - 3.5 Position of sun at time when earth is at aphelion

OM-MSS Section - 3.5

SUN Positional Parameters on Celestial Sphere : Input Year Time when Earth is at Aphelion .

5. Finding Position of Sun on Celestial Sphere at Input Universal Time, when Earth is at Aphelion .

Input Universal Time Corresponds to Earth at Aphelion : year = 2013, month = 7, day = 5, hour = 0, minute = 18, seconds = 52.59269

Output : Sun Position on Celestial Sphere Corresponding to input time, Earth reaching Aphelion

| | | | | | |
|--|---|-----------------|--|---|-----------------|
| 01. Earth around Sun Mean motion rev per day (mm) | = | 0.0027377786 | 02. Semi-major axis in km considering oblateness (SMA) | = | 149598616.31172 |
| 03. Earth mean motion deg per day using SMA (mm) | = | 0.9856003000 | 04. Sun mean movement deg per day (n sun) | = | 0.9856003000 |
| 05. Eccentricity of earth orbit (e sun) | = | 0.0167102190 | 06. Perihelion to input time diff in Julian days | = | 182.6298145405 |
| 07. Mean anomaly in deg per day from n_sun (m sun) | = | 180.0000000001 | 08. Sun Mean Longitude in deg (Lmean) | = | 103.1643684676 |
| 09. Earth Mean anomaly in deg (ME) | = | 180.0000000002 | 10. Sun Ecliptic Longitude in deg (Lsun) | = | 103.1643684676 |
| 11. Obliquity of ecliptic in deg (Epcylone) | = | 23.4375223935 | 12. Sun Right ascension in deg (Alpha) | = | 104.3014954901 |
| 13. Sun Declination in deg (Delta) | = | 22.7863704018 | 14. Sun Mean distance in km (As) | = | 149598616.31172 |
| 15. Sun Radial distance from earth in km (Rs) | = | 152098409.19029 | 16. Sun Nodal elongation in deg (U sun) | = | 76.8356315324 |
| 17. Sun Mean anomaly in deg (M sun) | = | 179.9999999997 | 18. Sun Eccentric anomaly in deg (E sun) | = | 179.9999999997 |
| 19. Sun True anomaly in deg (T sun) | = | 179.9999999997 | 20. Sun Argument of perigee in deg (W sun) | = | 256.8356315327 |
| 21. Sun True anomaly in deg from U & W (V sun) | = | 179.9999999997 | 22. Sun Distance in km (d sun) | = | 152098441.95238 |

Sun Ecliptic latitude is always nearly zero (the value never exceeds 0.00033 deg)

Next Section - 3.6 Position of sun at time when earth is at autumnal equinox

SUN Positional Parameters on Celestial Sphere : Input Year Time when Earth is at Autumnal equinox .

6. Finding Position of Sun on Celestial Sphere at Input Universal Time, when Earth is at Autumnal equinox .

Input Universal Time Corresponds to Earth at Autumnal equinox : year = 2013, month = 9, day = 22, hour = 20, minute = 45, seconds = 38.50711

Output : Sun Position on Celestial Sphere Corresponding to input time, Earth reaching Autumnal equinox

| | | | | | |
|--|---|-----------------|--|---|-----------------|
| 01. Earth around Sun Mean motion rev per day (mm) | = | 0.0027377786 | 02. Semi-major axis in km considering oblateness (SMA) | = | 149598616.31172 |
| 03. Earth mean motion deg per day using SMA (mm) | = | 0.9856003000 | 04. Sun mean movement deg per day (n sun) | = | 0.9856003000 |
| 05. Eccentricity of earth orbit (e sun) | = | 0.0167102190 | 06. Perihelion to input time diff in Julian days | = | 262.4817348463 |
| 07. Mean anomaly in deg per day from n_sun (m sun) | = | 258.7020766091 | 08. Sun Mean Longitude in deg (Lmean) | = | 181.8702061020 |
| 09. Earth Mean anomaly in deg (ME) | = | 258.7020766091 | 10. Sun Ecliptic Longitude in deg (Lsun) | = | 180.0000000001 |
| 11. Obliquity of ecliptic in deg (Epcylone) | = | 23.4374939503 | 12. Sun Right ascension in deg (Alpha) | = | 180.0000000001 |
| 13. Sun Declination in deg (Delta) | = | -0.0000000001 | 14. Sun Mean distance in km (As) | = | 149598616.31172 |
| 15. Sun Radial distance from earth in km (Rs) | = | 150128632.16764 | 16. Sun Nodal elongation in deg (U sun) | = | -0.0000000001 |
| 17. Sun Mean anomaly in deg (M sun) | = | 258.7020766085 | 18. Sun Eccentric anomaly in deg (E sun) | = | 257.7663930098 |
| 19. Sun True anomaly in deg (T sun) | = | 256.8323186392 | 20. Sun Argument of perigee in deg (W sun) | = | 103.1676813607 |
| 21. Sun True anomaly in deg from U & W (V sun) | = | 256.8323186392 | 22. Sun Distance in km (d sun) | = | 150048057.36583 |

Sun Ecliptic latitude is always nearly zero (the value never exceeds 0.00033 deg)

Next Section - 3.7 Position of sun at time when earth is at winter solstice

SUN Positional Parameters on Celestial Sphere : Input Year Time when Earth is at Winter solstice .

7. Finding Position of Sun on Celestial Sphere at Input Universal Time, when Earth is at Winter solstice.

Input Universal Time Corresponds to Earth at Winter solstice : year = 2013, month = 12, day = 21, hour = 17, minute = 10, seconds = 3.73442

Output : Sun Position on Celestial Sphere Corresponding to input time, Earth reaching Winter solstice

| | | | | | |
|--|---|-----------------|--|---|-----------------|
| 01. Earth around Sun Mean motion rev per day (mm) | = | 0.0027377786 | 02. Semi-major axis in km considering oblateness (SMA) | = | 149598616.31172 |
| 03. Earth mean motion deg per day using SMA (mm) | = | 0.9856003000 | 04. Sun mean movement deg per day (n sun) | = | 0.9856003000 |
| 05. Eccentricity of earth orbit (e sun) | = | 0.0167102190 | 06. Perihelion to input time diff in Julian days | = | 352.3320268290 |
| 07. Mean anomaly in deg per day from n_sun (m sun) | = | 347.2585513424 | 08. Sun Mean Longitude in deg (Lmean) | = | 270.4309127840 |
| 09. Earth Mean anomaly in deg (ME) | = | 347.2585513424 | 10. Sun Ecliptic Longitude in deg (Lsun) | = | 269.9999511320 |
| 11. Obliquity of ecliptic in deg (Epcylone) | = | 23.4374619456 | 12. Sun Right ascension in deg (Alpha) | = | 269.9999467376 |
| 13. Sun Declination in deg (Delta) | = | -23.4374619456 | 14. Sun Mean distance in km (As) | = | 149598616.31172 |
| 15. Sun Radial distance from earth in km (Rs) | = | 147162417.75585 | 16. Sun Nodal elongation in deg (U sun) | = | -90.0000000000 |
| 17. Sun Mean anomaly in deg (M sun) | = | 347.2585513416 | 18. Sun Eccentric anomaly in deg (E sun) | = | 347.0438922873 |
| 19. Sun True anomaly in deg (T sun) | = | 346.8274560675 | 20. Sun Argument of perigee in deg (W sun) | = | 283.1725439325 |
| 21. Sun True anomaly in deg from U & W (V sun) | = | 346.8274560675 | 22. Sun Distance in km (d sun) | = | 147158348.89183 |

Sun Ecliptic latitude is always nearly zero (the value never exceeds 0.00033 deg)

Thus Computed values for Position of Sun on Celestial Sphere corresponding to Standard Epoch time JD2000, and six astronomical events while earth reaches Perihelion, Vernal equinox, Summer solstice, Aphelion, Autumnal equinox, Winter solstices.

Move on to Summary of these Computed values are presented next.

Next Section - 3.8 Concluding Position of Sun at six astronomical events.

Concluding Position of Sun on Celestial Sphere (Sections 3.0 to 3.7)

Concluding Sun Position on Celestial Sphere with respect to Earth orbit, in the Year = 2013, at six astronomical events.

In previous Sections (3.1 to 3.7), the position of Sun on Celestial Sphere were represented by computing following parameters :

Orbit Semi-major axis (SMA), Mean movement per day (n sun), Mean distance (As), Mean anomaly (m sun), True anomaly (T sun), Eccentric anomaly (E sun), Right ascension (Alpha), Declination (Delta), Mean Longitude (Lmean), Ecliptic Longitude (Lsun), Nodal elongation (U sun), Argument of perigee (W sun), Obliquity of ecliptic (Epcylone), Mean dist (d_sun), Radial distance (Rs).

All these parameters were computed while Earth moves around Sun and reaches six astronomical event points :

Perihelion, Vernal equinox, Summer solstice, Aphelion, Autumnal equinox, Winter solstice .

Summary of Sun Position on Celestial Sphere with respect to Earth while moved around Sun, passed through at six astronomical events.

| Universal time while earth at | Mean anom M_sun | True anom T_sun | Ecce.anom E_sun | Right asc. Alpha | Declina Delta | Mean log. L_mean | Ecli.log. L_sun | Nodal elon. U_sun | Arg of peri w_sun | Obliquity Epcylone | Mean dist. d_sun | Radial dist. Rs |
|-------------------------------|-----------------|-----------------|-----------------|------------------|---------------|------------------|-----------------|-------------------|-------------------|--------------------|------------------|-----------------|
| Perihelion | 0.00 | 0.00 | 0.00 | 284.29 | -22.79 | 283.16 | 283.16 | -76.84 | 283.16 | 23.44 | 147098790.67 | 147098823.43 |
| Vernal equinox | 74.98 | 76.84 | 75.91 | 0.00 | 0.00 | 358.14 | 0.00 | 0.00 | 283.16 | 23.44 | 148912015.97 | 148989898.68 |
| Summer solstice | 166.39 | 166.84 | 166.62 | 90.00 | 23.44 | 89.56 | 90.00 | 90.00 | 283.16 | 23.44 | 152025947.60 | 152030583.04 |
| Aphelion | 180.00 | 180.00 | 180.00 | 104.30 | 22.79 | 103.16 | 103.16 | 76.84 | 256.84 | 23.44 | 152098441.95 | 152098409.19 |
| Autumnal equinox | 258.70 | 256.83 | 257.77 | 180.00 | -0.00 | 181.87 | 180.00 | -0.00 | 103.17 | 23.44 | 150048057.37 | 150128632.17 |
| Winter solstice | 347.26 | 346.83 | 347.04 | 270.00 | -23.44 | 270.43 | 270.00 | -90.00 | 283.17 | 23.44 | 147158348.89 | 147162417.76 |

Orbit Semi-major axis in km (SMA) = 149598616.31172, Eccentricity (e sun) = 0.0167102190
 Mean movement deg per day (n sun) = 0.9856003000, Mean distance from earth in km (As) = 149598616.31172

Continue Section - 2.8

In the table above , all angles are in deg and distances in km. The values show consistency. About accuracy, for an input Universal Time, Compared below the computed values against that reported (Ref. <http://www.stargazing.net/kepler/sun.html>).

For Input Universal Time year = 1997, month = 8, day = 7, hour = 11, minute = 0, seconds = 0.000000000 (under reference)

The Output **Computed values** : Sun Position on Celestial Sphere at Input UT time

- 07. Sun Mean anomaly in deg per day from n_sun (m sun) = 213.1154702210
- 08. Sun Mean longitude in deg (Lmean) = 136.0061615585
- 10. Sun Ecliptic longitude in deg (Lsun) = 134.9782467378
- 11. Obliquity of the ecliptic plane in deg (Epcylone) = 23.4395921140
- 12. Sun Right ascension in deg (Alpha) = 137.44256792552
- 13. Sun Declination in deg (Delta) = 16.3426505298

The Output **Reported values** : Sun Position on Celestial Sphere at same UT time, (Ref. <http://www.stargazing.net/kepler/sun.html>).

- 07. Sun Mean anomaly in deg per day from n_sun (m sun) = 213.11547
- 08. Sun Mean longitude in deg (Lmean) = 136.00716
- 10. Sun Ecliptic longitude in deg (Lsun) = 134.97925
- 11. Obliquity of the ecliptic plane in deg (Epcylone) = 23.439351
- 12. Sun Right ascension in deg (Alpha) = 137.44352
- 13. Sun Declination in deg (Delta) = 16.342193

End of Computing Position of Sun on Celestial Sphere at Standard Epoch JD2000 and at Six Astronomical Events.

Move on to Compute the Position of Earth on Celestial Sphere at Input Universal Time (UT).

Next Section - 4 Position of Earth on Celestial Sphere at UT

REFERENCES : TEXT BOOKS & INTERNET WEB LINKS.**Books**

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Internet Weblinks**Ref. Sec 3 Position Of Sun On Celestial Sphere**

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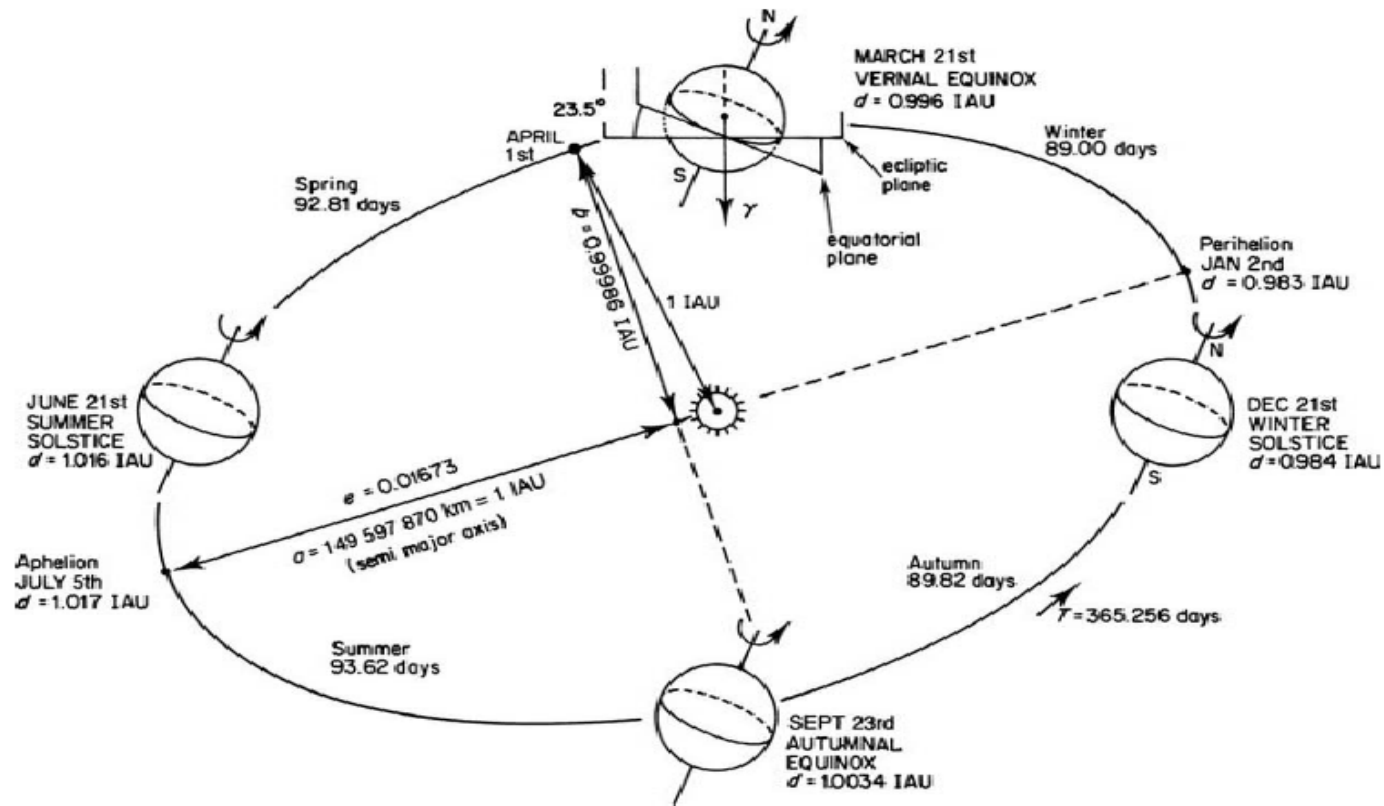


Fig-3. Orbit of Earth Around Sun

Earth rotates around sun with a period of approximately 365.25 days following an Ellipse of Eccentricity 0.01673 and Semi-major axis 149597870 km, which defines the Astronomical unit of distance (AU). Around 2 January, Earth is nearest from sun called **Perihelion** while around 5 July it is farthest from Sun called **Aphelion** (around 152100000 km). The other events point are **Vernal equinox** around 21 March, **Autumnal equinox** around 23 September, **Summer solstice** around 21 June and **Winter solstic** around 21 December. The plane of the orbit is called the plane of the Ecliptic that makes an angle 23.44 deg (the Obliquity of the Ecliptic) with the mean Equatorial plane.

Source Book by Gerard Maral, Michel Bousquet, 'Satellite Communications Systems', Fifth Edition, John Wiley & Sons, chap. 2, Pg 29, 2002.

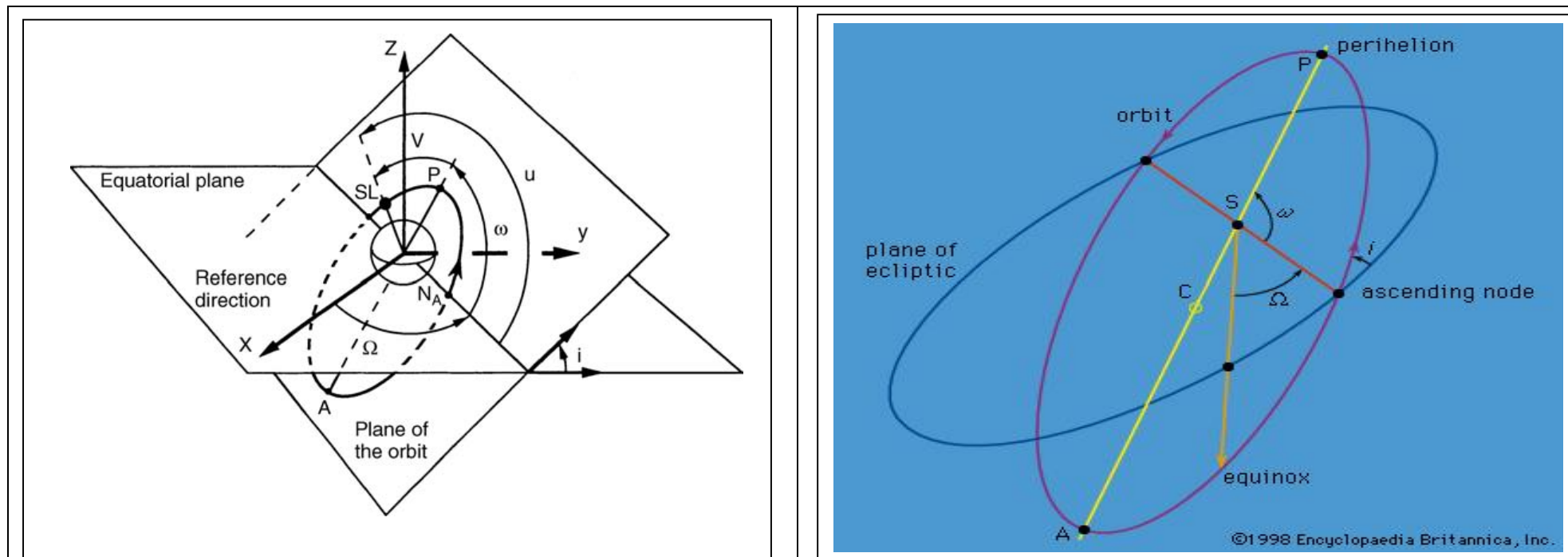


Fig- 4 & 5 Positioning of Orbit in Space

Orbit Position in Space at Epoch is defined by the Values of Kepler Orbit elements : (definitions apply to both planets & Satellites)

1. **Inclination 'i'** of the orbit of a planet, is angle between the plane of planet's orbit and the plane containing Earth's orbital path (ecliptic).
2. **Right ascension 'Ω'** of the ascending node is the angle taken positively from 0 to 360 deg in the forward direction, between the reference direction and the ascending node of the orbit (the intersection of the orbit with the plane of the equator crossing this plane from south to north).
3. **Argument of Perigee 'ω'**, specify angle between orbit's perigee and orbit's ascending node, measured in orbital plane and direction of motion.
4. **Eccentricity 'e'** of an orbit shows how much the shape of an object's orbit is different from a circle;
5. **Mean Anomaly 'v'** relates the position and time for a body moving in a Kepler orbit. The mean anomaly of an orbiting body is the angle through which the body would have traveled about the center of the orbit's auxiliary circle. 'M' grows linearly with time.

A knowledge of above five parameters completely defines the trajectory of an object or satellite in space. However, the **Nodal angular elongation 'u'** can also be used to define the position of the satellite in its orbit. This is the angle taken positively in the direction of motion from 0 to 360 deg between the direction of the ascending node and the direction of the satellite ($u = \omega + v$).

Source Book by Gerard Maral, Michel Bousquet, 'Satellite Communications Systems', Fifth Edition, John Wiley & Sons, chap. 2, Pg 29, 2002. & <http://www.britannica.com/EBchecked/topic/101285/celestial-mechanics/images-videos/2285/orbital-element-keplers-laws-of-planetary-motion>